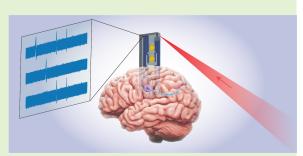


LiNbO3-based Synaptic Sensors via Microring Resonator Modulators

Ceren Babayigit, Rahim Esfandyarpour, and Ozdal Boyraz,

Abstract—The precise measurement of action potentials with high sensitivity and broad bandwidth is crucial in neuroscience research. However, current electrode-based methods are limited by bandwidth, sensitivity to biological noise, and tissue damage caused by measurement byproducts. To address these challenges, we propose a novel optrode that leverages the electro-optic (EO) effect of lithium niobate to detect electric fields generated by voltage differences in the extracellular medium. This new approach combines the EO effect with a ring resonator and coherent balance detector, enabling highly sensitive and precise action potential measurements. We demonstrate the feasibility of this opto-probe by carrying the signal with modulation and beating it through coherent detection to



detect weak signals. The array configuration of the sensor offers multiplexed sensing capabilities, enabling simultaneous detection of neural activity from multiple locations within the brain. Also, since light is used for measurements, the optrode does not generate heat or produce toxic byproducts, preventing tissue damage. The designed EO ring resonator exhibits a quality factor of approximately 10^4 , allowing for the sensing of action potentials as small as $15~\mu V$. Hence, the proposed method has the capability to overcome the limitations of current electrode-based methods, facilitating more accurate measurements of action potentials, and advancing the understanding of neuronal activity in the brain.

Index Terms— Electro-optic effect, Lithium niobate, Neuroprosthetics, Optical modulators, Optogenetics, Ring resonator modulators, Synaptic sensors.

I. INTRODUCTION

N recent years, neuroscience research has made significant strides in studying the brain and the nervous system. Our understanding of the nervous system is further enhanced by utilizing cutting-edge sensor technologies that can deliver precise spatiotemporal information across extensive spatial domains. However, the precise measurement of action potentials, the electrical signals generated by neurons, with high spatiotemporal resolution remains a significant challenge. Since electrodes are well known for the measurement of electrical signals, the current approaches heavily rely on electrodes to measure action potentials and synaptic activities of neurons [1]. Two prominent electrode array technologies, namely the Michigan and Utah arrays, have played a pivotal role in advancing our understanding of neural activities. The Michigan electrode array consists of a silicon-based platform with

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multiple shank electrodes, enabling simultaneous recording from multiple neurons with enhanced spatial resolution up to 35 electrodes/mm² [2]. On the other hand, the Utah electrode array features a flexible substrate (e.g., polyimide) and multiple penetrating electrode designs, allowing for precise and chronic neural recordings with a spatial resolution of up to 6 electrodes/mm² [3]. These cutting-edge electrode arrays represent significant advancements in neuroscience and hold promise for revolutionizing our understanding of brain function and its clinical applications. However, it is important to note that the relationship between the size of recording sites and impedance is inversely proportional, resulting in smaller electrodes being inherently noisier and displaying low recording quality. When dealing with weak signals such as action potentials, obtaining recordings with minimal noise and high quality is crucial. Hence, the need for sensors with better performance and long-term stability is still open to investigation to be relevant to applications like brain-machine interfaces.

Optogenetics, calcium imaging, the use of voltage-sensitive labels, and electric field (*E*-field) sensors are alternative approaches that can be used to measure action potentials. Optogenetics uses the response of genetically modified neurons to light. This modification enables their activation or inhibition through exposure to light, while simultaneously recording their responses [4]. Calcium imaging captures the changes in the concentration of calcium ions within cells to indirectly mea-

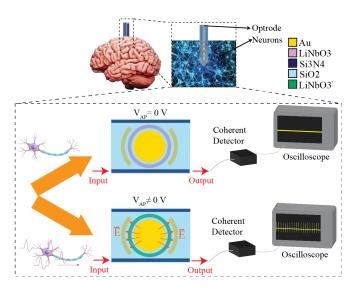


Fig. 1. Basic operating principle of the proposed optrode. Action potentials induce an electric field creation across the LiNbO $_3$ waveguide and result in a refractive index change of LiNbO $_3$. That creates light modulation which is extracted by the coherent detection to map electrical activity.

sure action potential [5]. In the case of voltage-sensitive dyes, changes in the electrical potential across the cell membrane labeled with voltage-sensitive markers are used as a direct method for monitoring neural activity [6]. Despite their advantages, these optical methods face limitations, such as restricted recording duration due to photobleaching, potential generation of phototoxic free radicals, and alterations in membrane electrical properties. Also, these approaches are not widely used in practice due to their complexity. On the other hand, (E-field) sensing is preferred for many healthcare monitoring due to its label-free nature, motion tolerance, and immunity to interference from other radio frequency (RF) services. If a proper probe design is provided, the same technique can be used for brain or tissue monitoring. According to Hales [7] and Cifra et. al [8], when an action potential occurs, it creates electromagnetic fields within the brain. This neuronal process causes membrane depolarization, resulting in ions' exit from the cell membrane. As these ions move, they generate ion currents that produce an electric field that is perpendicular to their direction of movement, in accordance with the righthand rule. The detection of this electric field can be mapped to neural activities, as presented in [9] by Balch et al.

In this work, we propose and investigate how to capture the (E-field) generated by synaptic activities by leveraging the electro-optic (EO) effect of lithium niobate (LiNbO₃). The ambient electric field will be weak, and the direction will be random. The EO effect, on the other hand, favors the (E-field) along certain orientations to induce a measurable phase change in the propagating optical field. Here, we investigate the method of detecting the weak (E-field) resulting from action potentials by sensing voltage variances in the extracellular medium. The proposed design pairs the unique electro-optic properties of LiNbO₃ micro-ring resonators (MRR) with a coherent detection scheme (see Fig.1) to capture synaptic activities in real-time with μV voltage sensitivity and up to

249 electrodes/mm² spatial resolution. We show that single neuron resolution imaging with a current detector output by capturing 15µV action potentials which corresponds to an Efield strength of 4.2 V/m. Diverging from traditional direct measurements of neural signals, the proposed design adeptly employs light modulation to convey the signal, which is subsequently processed through coherent detection. In essence, instead of relying on ambient (E-fields), our method utilizes extracellular action potentials to create a strong, directional, and uniform (E-field). This departure from ambient conditions ensures a more controlled and precise measurement environment, distinct from the random directional variations present in ambient field measurements. This method allows for detecting subtle differences in the E-field generated by neurons, enabling us to record their activity without the need for exogenous labels. Further, it mitigates susceptibility to electrical and biological noise consequently reducing signal loss and enhancing sensitivity. This method could potentially pave the way for exploring the complex dynamics within neuronal networks, offering potential advancements in comprehending how the nervous system operates.

Up to date, optical E-field sensors (optrode) have been proposed as an alternative approach for conventional applications outside the biomedical field due to their benefits, such as minimal interference with the E-field being measured, the ability to measure a wide range of dynamic signals, a broad frequency response, and a high level of sensitivity. The fundamental operating mechanism of the most widely used optical E-field sensors are classified into two categories: the inverse piezoelectric effect [10] and the EO effect [11]. The inverse piezoelectric effect involves the generation of an Efield in response to mechanical stress or deformation of a material. In an optical E-field sensor based on this effect, a piezoelectric material is placed in an E-field and the resulting mechanical deformation of the material is measured using an optical technique such as interferometry. The magnitude of the E-field can be calculated based on the amount of deformation. On the other hand, the EO effect involves the modification of the refractive index of a material in response to an E-field exposure. In an optical E-field sensor based on this effect, a material with an EO coefficient is placed in an E-field and the resulting change in the refractive index is measured. The magnitude of the E-field can be calculated based on the amount of refractive index change. EO effect E-field sensors are generally considered superior to piezoelectric effect E-field sensors due to their higher sensitivity, wider dynamic range [12], higher linearity and non-invasive nature making them particularly suitable for applications requiring high precision.

Optical sensors based on the EO effect, such as the Mach-Zehnder interferometer, surface plasmon resonance sensors [13], fiber optic sensors, and MRR, have shown remarkable performance and potential for integration into photonic circuits. MRRs, in particular, have drawn considerable attention due to their compact size, high-quality factor (*Q*-factor), and wavelength selectivity, making them ideal for a range of applications, including filtering, sensing, mode-locking, electrooptic modulation, optical memory, and optical switches [14]–[20]. In recent years, various material systems have been

explored for MRR structures, including graphene [18], silicon, indium phosphide, polymer, and lithium niobate [21]–[24]. Among these materials, LiNbO₃ has emerged as a promising candidate for *E*-field sensing applications, owing to its large linear EO coefficient, high modulation speed, and stable chemistry [25], [26]. In biosensing, LiNbO₃ ring resonators have primarily been utilized for detecting changes in the refractive index of surrounding materials, such as glucose [27], without tapping into the material's EO effect. However, our research departs from this trend by exploiting LiNbO₃ 's EO properties to detect neural action potentials. Here, we present how we can utilize the large EO coefficient of LiNbO₃ for brain research and pave the way for further developments in brain-machine interfacing.

The paper is organized as follows: In Section 2, the structural design of the proposed LiNbO₃ MRR sensor and its operating principles are explored. Then the temporal and spectral analyses of the proposed design are presented. Section 3 analyzes the insights into the signal modulation through the LiNbO₃ MRR structure. A possible experimental platform with the coherent detection scheme is given in Section 4 along with detailed analyses of the probable action potential values. In Section 5, we present multi-array designs, followed by a discussion (Section 6) on why electro-optic resonators are feasible for the design while semiconductors are not. Finally, the summary of the study is provided in the Conclusion section.

II. THE DESIGN APPROACH AND PRINCIPLE OF OPERATION

The MRR sensors are known to be excellent tools for capturing weak perturbations in the refractive index of the surrounding medium [15]. Here we are not interested in the refractive index change of the surrounding material, but in capturing the refractive index changes in the sensor material due to neural activities. Also, resonant structures are known to be more sensitive to weak perturbations. Hence, we designed a synaptic sensor based on LiNbO₃ MRRs for highsensitivity detection of the E-field generated by the action potential. The proposed optrode structure consists of a LiNbO₃ MRR on a silicon dioxide (SiO₂) substrate as a reliable and stable platform (see Fig.2). The MRR structure has two gold electrodes to capture action potentials. The first electrode is buried in the SiO₂ layer and serves as a reference electrode. The second electrode, the inner gold plate, is exposed to neurons and it captures the action potential and creates an electric field between the two electrodes since it is in contact with the surrounding medium and neurons to capture voltages created by neuron activities. The internal E-field induces a refractive index change in the LiNbO3 waveguide sandwiched between two electrodes. This modulation of refractive index leads to modulation of the input light as it passes through the MRR structure, ultimately allowing for the detection of the electrical activity of neurons. The detection mechanism is a critical aspect of the optrode's design, and it employs a coherent detection system to achieve high sensitivity and accuracy. To assess the sensitivity of the proposed system we

built an analytical model based on an MRR sensor with a double bus configuration, as shown in Figure 2 (a). Here, the corresponding outer radius of LiNbO $_3$ is adjusted as $R_{\rm out}$ = 20 μ m. Dimensions are comparable to the size of a single neuron. Hence, it shows that such sensors have the capability of detecting single-cell activities and potentially they can achieve high spatial resolution. The in-and-out light coupling from the LiNbO $_3$ ring is performed by silicon nitride (Si $_3$ N $_4$) bus waveguides.

To operate in a single mode, the widths of the LiNbO₃ and Si₃N₄ bus waveguides are determined using finite-difference time-domain (FDTD) mode analyses shown in Figs. 2(b) and 2(c) by using Lumerical simulation tool. The optimized width of the LiNbO₃ waveguide, which yields the highest Q-factor in single mode, is found to be t_2 = 0.63 μ m, while the widths of Si_3N_4 bus waveguides are set as t_1 = 1 μ m. As a result, we obtained the inner radius as $R_{\rm in}$ = 19.37 μm . To achieve optimal coupling between the waveguides, the gap between the LiNbO3 waveguide and the Si3N4 bus waveguides is set to $g_1 = 0.15 \mu m$. The inner gold plate which is in contact with the exterior medium has a radius of $R_e = 17.87 \,\mu\text{m}$ that leaves 1.5 μm spaces (g₂) between the LiNbO₃ waveguide. The outer gold plate which serves as the reference has a thickness of $t_3 = 2 \mu m$ with a spacing of $g_3 = 1.5 \mu m$ from the LiNbO₃ waveguide. Further, the thickness of the structure is set as h= 0.5 µm for all components. It has been previously demonstrated that the fabrication of LiNbO₃ is attainable within a thickness range spanning from 400 nm to 900 nm [28]–[30]. Finally, to ensure that unwanted interference or distortion does not occur, the unused ends of the waveguides can be coated with perfectly matched layers (PML) or tapered.

The main sensor architecture is an add-drop filter consisting of two waveguides situated on opposite sides of a ring resonator, as illustrated in Figure 2(a). The function of the lower the one waveguide is to introduce light into the resonators, while the upper waveguide is responsible for extracting light from the resonator. The optical resonance can be observed at two output ports. The pass-port, located at the opposite end of the input port, is the first waveguide in the add-drop structure. At the resonance wavelength, a dip in the transmission is observed in the pass-port. The drop-port, serving as the second output in the add-drop structure, exhibits a reverse transmission response compared to the add-port. It demonstrates transmission peaks at the resonant wavelengths.

The static transmission to both the pass-port and the dropport can also be represented for continuous wave (CW) operation by matching the fields as follows [31], [32]:

$$T_{pass} = \frac{I_{pass}}{I_{input}} = \frac{\tau_2^2 a^2 - 2\tau_1 \tau_2 a cos(\theta) + \tau_1^2}{1 - 2\tau_1 \tau_2 a cos(\theta) + (\tau_1 \tau_2 a)^2}.$$
 (1)

$$T_{drop} = \frac{I_{drop}}{I_{input}} = \frac{(1 - \tau_2^2)(1 - \tau_1^2)a}{1 - 2\tau_1\tau_2 acos(\theta) + (\tau_1\tau_2 a)^2}.$$
 (2)

where θ is the phase shift of the light after one round-trip inside the ring, a is the amount of attenuation of light after one round-trip, and τ_i is the self-coupling coefficient between LiNbO₃ ring and Si₃N₄ waveguides.

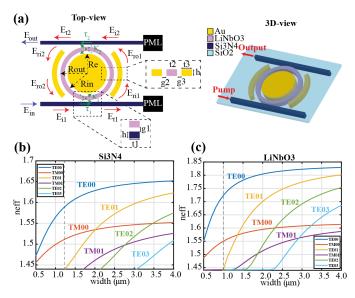


Fig. 2. (a) Schematic representation of electro-optic ring resonator-based synaptic sensor. Mode analyses of the (b) Silicon Nitride (Si $_3$ N $_4$) and (c) Lithium niobate (LiNbO $_3$) waveguides.Here the height of the waveguides is set as 0.5 μm and the width is swept from 0.5 μm to 4 μm .

For illustration purposes here we present analysis based on signal reading at the drop-port. The FDTD simulations are performed utilizing the parameters specified in Section 2, followed by the transmission measurement at the drop port. The observed spectral response of the MRR sensor is represented in Figure 3(a). The transmission peaks exhibit a free spectral range (FSR) of 0.9440 THz and a Q-factor of 8.9756×10^3 . To see resonance mode transmission through the drop port, cross-sectional intensity field distributions along the xy-plane are represented in Figs. 3(b) and 3(c) for the selected frequency values of f=192.5 THz (point A) and f=193.906 THz (point B). The labeled letters superimposed in Figure 3(a) indicate the frequency location in the transmission spectrum of the MRR. As expected, a noticeable enhancement in intensity is observed at the drop port when reaching the resonance point (referred to as B). Rather than operating at the resonance point, this proposed approach will bias the laser at the linear point of the transmission peak. This strategy aims to achieve a more sensitive response in detecting refractive index changes induced by the E-field. To determine this point, the derivative of the transmission peak centered at f=193.906THz is calculated and depicted in Fig. 3(d). Here the point, C, corresponding to f=193.951 THz is the linear point that gives the highest change in the transmission output. Since the MRR is biased at the quadrature point, the drop port intensity is also at its midpoint, as shown in Fig. 3(e).

III. SIGNAL MODULATION VIA LINBO3 MRR

The ring resonator steady-state transfer function is derived theoretically by describing the relation between electromagnetic waves in the straight waveguides before and after coupling regions (see Fig.2). We have two coupling regions which

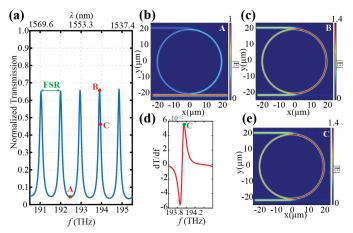


Fig. 3. (a) Transmission spectra of the synaptic sensor. Steady-state electric field intensity distributions for the (b) at f=192.5 THz (point A) and (c) at f= 193.906 THz (point B). (d) Derivative of the transmission spectra with respect to frequency for a focus range. (e) Electric field intensity distributions for the bias point at f=193.951 THz (point C).

are modeled by coupling matrices as follows:

$$\begin{bmatrix} E_{t1} \\ E_{ri1} \end{bmatrix} = \begin{bmatrix} \tau_1 & i\kappa_1 \\ i\kappa_1 & \tau_1 \end{bmatrix} \begin{bmatrix} E_{i1} \\ E_{ro1} \end{bmatrix}$$
 (3)

$$\begin{bmatrix} E_{t2} \\ E_{ri2} \end{bmatrix} = \begin{bmatrix} \tau_2 & i\kappa_2 \\ i\kappa_2 & \tau_2 \end{bmatrix} \begin{bmatrix} E_{i2} \\ E_{ro1} \end{bmatrix}$$
 (4)

where the amplitude cross-coupling and self-coupling coefficients are given by κ_i and τ_i respectively, and $|\kappa_i|^2 + |\tau_i|^2$ =1. Note that the cross-coupling and self-coupling coefficients for both ports are identical, hence they can be represented as $\kappa = \kappa_1 = \kappa_2$ and $\tau_i = \tau_1 = \tau_2$. After generating the input wave, a fraction of it is coupled into the resonator to form a traveling wave that circulates clockwise around the ring. During a single round-trip around the ring, the circulating wave experiences attenuation due to intrinsic optical losses. The attenuation factor can be expressed as $a^2 = \exp(-\alpha L)$, where α is the attenuation coefficient in the ring and L is the total circumference of the ring. The traveling wave that circulates in a clockwise direction around the ring also undergoes a phase shift, denoted by θ , which can be expressed as θ = ωT , where ω represents the angular frequency of the input field and T is the round-trip travel time of the ring. The round-trip travel time, denoted by T, is given by T = nL/c, where n is the effective refractive index of the ring, L is the ring's circumference, and c represents the vacuum light speed. In the case of LiNbO₃, the material's refractive index varies depending on the electric field induced by the neurons. Hence it can be shown as $n(V(t))=(n_0-\frac{1}{2}n_0^3r_{13}\frac{V(t)}{d})$ where d is the spacing between the electrodes, n_0 is the effective refractive index of the propagating mode, and r₁₃ is the electrooptic coefficient of the LiNbO3. Then, the phase shift can be rewritten as follows $\theta(t)=2\pi/\lambda$ n(V(t))L. By using the given relations, the static field transfer function of the double bus MRR system for the drop port can be written as:

$$\frac{E_{out}}{E_{in}} = \frac{-(1-\tau^2)\sqrt{a}e^{j\theta(t)/2}}{\tau(1-ae^{j\theta(t)})}$$
 (5)

Optical modulation in a microring resonator is accomplished by modulating the refractive index of the resonator, which can be achieved by varying the applied voltage V(t), or equivalently, the effective refractive index n(t). The action potential induced by the neurons produces a time-varying refractive index modulation, which gives rise to intensity modulation in the output of the resonator. Hence, the dynamic transfer function of the MMR is essential for characterizing its response to time-varying input signals. The dynamic transfer function of the MMR provides information on how the resonator responds to changes in its input signal, including changes in frequency and amplitude. If we define the static output signal as:

$$s_{out}(t) = E_{in} \frac{-(1-\tau^2)\sqrt{a}e^{j\theta(t)/2}}{\tau(1-ae^{j\theta(t)})}$$
 (6)

Then we can define the output signal after the dynamic response as follows:

$$s_{out_{dynamic}}(t) = A_{in}[cos(2\pi f_{in}t) + mcos(2\pi f_{m}t + \phi_{m})cos(2\pi f_{in}t)]$$
(7)

where $m(t) = \frac{|s_{out}(t)|}{A_{in}}$. Thus, the time-varying signal at the end of the drop port, after the modulation induced by the action potential, is defined by (7). By solving it, we can accurately predict the response of the LiNbO₃ ring resonator to the action potential.

IV. POTENTIAL EXPERIMENTAL SCENARIO WITH COHERENT DETECTION

The optical characterization of the proposed system can be carried out via coherent detection of the modulated signal. As illustrated in Fig.4(a), the experimental scenario with a coherent detection system. We start with a laser beam that is split into two branches: the signal beam and the reference or local oscillator beam. Subsequently, the signal beam is coupled to the waveguide and resonator. As a result, the resonator will experience the modulation induced by the neuron action potential as defined in (7) and generate the E-field presented in (S1). The modulated signal is then coupled out of the resonator and directed to the coherent detection system. The unmodulated reference beam with an E-field profile in (S2) is directed onto the coherent detection system where the reference beam acts as a local oscillator. The interfering signal beam and the local oscillator signal are then converted to photocurrent by a balanced detector. The resultant differential photocurrent generated by the matched detectors can be expressed as follows [33]:

$$I(t) = 2R\sqrt{P_{in}P_{lo}}cos(\phi_{in} + \phi_{lo}) + mcos(2\pi f_m t + \phi_m + \phi_{in} + \phi_{lo})$$
(8)

By beating the modulated signal induced by the action potential with the reference signal, the system can accurately detect and quantify the neural activity. The literature reports that action potentials generated by neurons typically exhibit an amplitude ranging from 30 μV to 100 mV, and a period in the range of 0.6 to 0.1 seconds (see Table.I). Based on the reported amplitude and frequency range of action potentials in the literature, we conducted a comprehensive analysis of

detectability of the neural activities. In our initial analysis, we focus on assessing the signal-to-noise ratio (SNR) of the generated electrical signal for different optical power values and under 30 μV action potential excitation. For this study, we limit the detection (noise) bandwidth (BW) to 1 kHz, and we set the RIN of the laser at a constant level of -160 dB/Hz. The SNR calculations include the shot noise and thermal noise generated by the detector and the relative intensity noise (RIN) of the source laser as described in (9). The phase noise of the laser and the dark current are ignored in this case.

$$SNR = \frac{I^2}{\sigma_S^2 + \sigma_T^2 \sigma_R I N^2}$$

$$= \frac{I^2}{2qRP_{avg}\Delta F + \frac{4K_BT}{R_L}\Delta F + (RP_{avg})^2 10^{\frac{RIN(f, P_{avg}}{10}}\Delta F}, where RIN(f, P_{avg}) = \frac{S_{\delta P}(f)}{P_{avg}^2}$$
(9)

Here, q is the electron charge, ΔF is the electrical detection bandwidth or noise bandwidth, K_B is the Boltzmann constant, T is the temperature (K), R_L is the load resistance, $S_\delta P$ (f) is the power spectral density, f is the frequency and RIN (in linear scale) is the relative intensity noise of the laser. It's important to know that increasing the pump's power can make the laser more stable and reduce the RIN in its output. So, practical scenarios may yield more favorable outcomes than those predicted by a simplistic linear assumption [34], [35].

Figure 4(b) illustrates a mesh plot depicting the SNR levels across a range of input and local oscillator power settings. Due to the power-dependent nature of shot noise and RIN, it becomes evident that by amplifying the local oscillator power, the system becomes RIN-dependent, and SNR will decrease in the simplistic model mentioned above. For local oscillator powers less than 2 mW, it is more shot noise dependent, and SNR improves with the local oscillator power. For a clearer demonstration of this characteristic, cross-sections have been extracted from the mesh plot at specific input powers of 0.2mW, 0.4mW, 0.6mW, 0.8mW, and 1mW, as indicated in Figure 4(c). In a subsequent analysis, the input power was fixed at 1mW, and the noise variances for thermal noise shot noise, and RIN were plotted while varying the local oscillator power. As depicted in Figure 4(d), it is evident that up to 2mW, the system is limited by shot noise, whereas beyond 2mW, the system becomes limited by RIN. Hence, due to the quadratic relationship between RIN and power, once the system transitions to being RIN-limited, the SNR experiences a rapid and pronounced decrease as seen in Fig.4(c). Following this comprehensive analysis, a fixed input power of 1mW and a local oscillator power of 2mW were identified as the optimal settings for subsequent analyses, as they resulted in the highest SNR values.

In our next analysis, we focus on assessing the SNR of the generated electrical signal for different values of action potential captured by the probe. This assessment is carried out by varying amplitude levels of the action potential from 30 μ V to 100 mV while maintaining a constant period of 1 millisecond. To assess the impact of the Q values of the

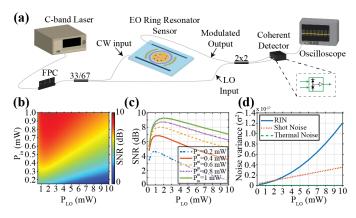


Fig. 4. (a) Schematic representation of the experimental scenario. (b) Mapping SNR in a plane (P_{lo},P_{in}) at 30 $\upmu V$ action potential amplitude. (c) Cross-sections extracted from the SNR map for different input power values. (d) Noise characteristics of the system for P_{in} =1 mW input power.

TABLE I
AMPLITUDE AND PERIOD INFORMATION OF ACTION
POTENTIALS OF DIFFERENT KIND OF NEURON CELLS

Ref.	Cell Type	Period	Amplitude
[36]	Hippocampal neurons	1.5-2.5 ms	100-200 μV
[37]	Monkey's Inhibitory	0.2-1 ms	30-100 mV
	cells		
[38]	Mammalian central	2 ms	20-40 mV
	neurons		
[39]	hiPSC-CM	0.1 s	3.56 mV
[40]	neocortex of rats	0.7 ms	120 μV
[41]	neurons in the nucleus	2 ms	8.38 mV
	laminarins		
[42]	hippocampal neurons	0.6 ms	30-50 μV
	from postnatal mice		

ring resonator, we vary the Q values from 10^2 to 10^5 in the same analysis. Here, we assume the optical power of the local oscillator at 2mW at the input of the 2x2 coupler, and the average signal power at the resonator input is 1mW. After passing through the ring resonator, the power observed at the input arm of the 2x2 coupler is 0.69 mW. As depicted in Figures 5(a) and (b), we observe that the sensor's sensitivity increased as the Q-factor value increased. The output current exhibited a range spanning from nanoamps to milliamps, demonstrating the sensor's ability to detect action potentials across a wide amplitude spectrum. Notably, O-factors greater than 10^2 can detect action potentials with amplitudes as small as 30 μ V. In cases where the Q-factor was equal to 10^2 , the 3dB SNR is achievable at 65 µV action potentials at the sensor. The same level of action potential at the sensor can generate 37dB SNR if a ring resonator with $Q = 10^5$ is used. 30 μ V action potential is detectable with 9 dB SNR if a ring resonator with Q of 10^3 is used. If we seek 24dB SNR we need to work with the ring resonator having Q of 10^4 .

Next, we have conducted a study on the impact of laser RIN on the detectability of the action potential. Here we assume the optical power levels are the same as before, and the Q value of the resonator is assumed to be $Q=10^3$. We investigate maximum tolerable laser RIN to achieve 3dB SNR at the detector. In practice, the detector bandwidths are larger than 100MHz. However, since our signal is in the order of

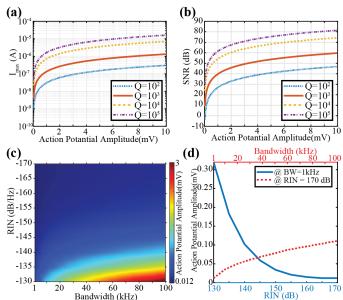


Fig. 5. (a) Variations in output current obtained via coherent detection relative to action potential amplitude for different *Q*-factor values. (c) Calculated SNR values of the system relative to action potential amplitude, with variations in *Q*-factor values. (d) Mapping detectable action potential amplitude in a plane (BW, RIN) at 3dB SNR. (e) Cross-sections extracted from the amplitude map at BW = 1kHz and RIN = -170 dB/Hz.

1kHz, we limit the noise bandwidth to up to 100 kHz in our analyses. Figure 5(c) presents the mesh plot of 3dB SNR for various detection bandwidths and RIN. As shown in the figure, a narrow linewidth laser with a RIN value of -160 dB/Hz, and a 3dB SNR is achievable at ~15 μV and ~147 μV action potentials by using detection bandwidths of 1kHz and 100kHz, respectively. By using a typical telecom grade DFB laser with -145dB/Hz RIN value, 3dB SNR is achievable at 60 μV action potentials with a detection bandwidth of 1 kHz. In the case of a 100 kHz detection bandwidth, the 3 dB SNR can be reached at approximately 580 μV action potentials.

Figure 5(d) presents the required RIN values and action potentials to achieve 3dB SNR at different detection bandwidths. As shown with the solid blue curve, ~47 μ V action potential is detectable if the noise bandwidth is 10kHz by using a -160 dB/Hz RIN value while ~185 μ V action potential is detectable by using a -145 dB/Hz RIN at the same bandwidth. Also, we present minimum detectable action potential for various noise bandwidth values by using an ultra-narrow linewidth laser with -170dB/Hz linewidth. In this case, the detectable amplitude values exhibit a range from ~12 μ V to ~110 μ V within a detection bandwidth that ranges from 1 kHz to 100 kHz.

From the outcomes of the aforementioned analyses, it's clear that one can tailor the sensor parameters to suit specific application requirements. As presented in Table.I, action potentials and their periods vary for different neuron types. Hence, depending on the targeted application, the required sensitivity and noise bandwidths change. For instance, while 1kHz noise bandwidth and 200 μV sensitivity are necessary for hippocampal neurons, mammalian central neurons can deliver as much as 20 μV action potential with 1kHz synapse rates.

Since the proposed system has a large dynamic range, it can be adapted to desired applications. This finding underscores the potential of the microring resonator sensor with coherent detection as a promising tool for the precise and accurate measurement of neural activity in various applications, including but not limited to neuroscience research, clinical diagnostics, and brain-machine interfaces.

V. ARRAY CONFIGURATION WITH LINBO₃ MMR

One type of neural probe that has gained significant attention in recent years is the multi-array electrode (MAE). MAEs are highly advanced devices that consist of an array of microelectrodes capable of simultaneously recording or stimulating neural activity from multiple locations within the brain. By recording the activity of large populations of neurons simultaneously, researchers can obtain a more comprehensive understanding of the brain's activity patterns and dynamics. Additionally, the ability to stimulate neural activity in precise patterns and locations using MAEs has opened up new possibilities for developing treatments for neurological disorders such as epilepsy and Parkinson's disease [43]. Several wellknown MAEs have been developed over the years, including the Utah array [3] and the Michigan probe [2]. One challenge with the Utah and Michigan array is that the spacing between the microelectrodes is relatively large (400 µm and 100 µm, respectively) compared to the size of individual neurons, which can limit the spatial resolution of recordings [44]. MAE systems, including the Utah and Michigan probes, also suffer from some noise in their recorded signals due to the use of wires to carry the electrical signals. Several sources of noise can affect the signals recorded by these probes, including electrical noise and signal attenuation. Electrical noise can come from a variety of sources, including power lines, electronic devices, and even the body's electrical activity and it can interfere with the small signals recorded by the electrodes, making it more difficult to extract meaningful information. Also, the electrical signals recorded by the electrodes can weaken as they travel through the wires, leading to a loss of signal strength and fidelity. To address these challenges, we propose an array structure with LiNbO₃ MRRs which has a 20 um diameter and 50 µm spacing distance as shown in Figs.6 (a) and (b). Since the proposed system uses the modulated optical signal to carry information rather than carrying the weak signal over a wire, it is more susceptible to noise and signal attenuation. Another important parameter for spatial resolution is the density of the electrodes. The commonly used Utah array typically includes 96 electrodes on a single array covering an area of 4mm by 4mm [45]. On the other hand, the Michigan array includes 64 electrodes on a single array covering an area of 0.6 mm by 3mm [40]. We propose the use of a single array containing 400 electrodes, which covers an area of 1.64 mm by 0.977 mm. This array is shown schematically in Fig. 6(b) in a one-row configuration. The spacing between the Si₃N₄ waveguides is taken as 500 nm which is specified in reference [46].

Upon conducting 3D FDTD analyses for the array configuration depicted in Figs. 6(c) and 6(d), we observed that both

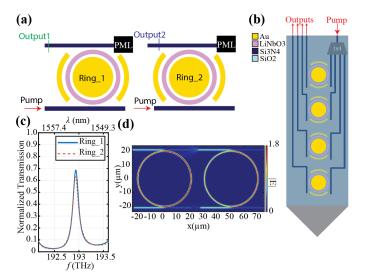


Fig. 6. (a) Schematic representation of electro-optic ring resonator-based synaptic sensor in an array configuration. (b) Schematic representation of optrode with array configuration. (c) Transmission spectra of the array configuration. (d) Steady-state electric field intensity distributions at *f*=192.938 THz.

ring resonators with a spacing of 50 μ m demonstrated identical responses at the same resonant frequency. This finding suggests that the proposed configuration may offer enhanced scalability and potential for multiplexed sensing applications, where multiple sensors can be arranged in an array format to enable simultaneous detection of multiple signals in parallel. The main drawback of the system is the power consumption, primarily due to the splitting of input power and the local oscillator into multiple paths (1xN configuration).

VI. DISCUSSION

Design of the MRR can also be conducted by using semiconductor material, such as silicon (Si). Silicon ring resonators play a crucial role in the field of photonics and integrated optics since their integration with other photonic components on a CMOS platform enables miniaturization and cost reduction, making them practical and scalable. With high-O factors and the ability to sustain resonant modes, silicon ring resonators ensure efficient light interaction and enhance sensitivity. However, due to the centrosymmetric crystal structure of Si, it does not exhibit a linear EO effect (Pockels). Soref and Bennet [47] have conducted investigations on Efield effects in Si to assess their effectiveness and it has shown that the Kerr effect [48]-[50] and the Franz-Keldysh effect are small in Si, too. Hence, to be able to obtain modulation in Si MRR, one should use the carrier depletion effect [47]. In this configuration, the ring resonator is biased in the depletion mode, creating a depletion region within the waveguide of the ring. This depletion region alters the effective refractive index of the waveguide, making it sensitive to changes in the E-field applied. When an external E-field is applied to the sensor, it modifies the width and depth of the depletion region, leading to a change in the effective refractive index of the waveguide. This change affects the resonance properties of the ring resonator.

Nevertheless, there are two main drawbacks to that configuration which make LiNbO3 more suitable for the proposed sensor design rather than Si. Firstly, temperature fluctuations can affect the performance of these sensors due to their reliance on the carrier concentration and dimensions of the depletion region. Temperature variations can alter the properties of the depletion region, leading to changes in the sensor's response and potentially introducing inaccuracies in the measured Efield. In Ref. [51], it has been demonstrated that brain temperature is not stable within the normal physiological and behavioral continuum but rather shows relatively large fluctuations (2-4 °C). Hence, to mitigate this issue, temperature compensation techniques or additional temperature sensors may be required to ensure accurate and reliable measurements. Secondly, depletion mode sensors require a continuous bias voltage to maintain the depletion region, resulting in continuous power consumption. The biasing conditions must be carefully addressed to achieve optimal performance. Moreover, it requires additional cabling in the design to sustain the biasing. Thus, while semiconductor materials like silicon may exhibit promising quality factor values, their practical limitations make them less conducive to certain applications such as action potential measurements. In this direction, with its high EO coefficient LiNbO₃ is preferred to be used in the proposed design to illustrate the potential of EO crystals in neuroscientific research.

VII. CONCLUSION

In conclusion, this study presents a novel optrode design that utilizes the EO effect of LiNbO₃ to enable highly sensitive and precise measurement of action potentials in neuroscience research. The proposed optrode combines the EO effect with a ring resonator and coherent balance detector, allowing for the detection of subtle changes in the refractive index induced by neuronal activity. The optrode offers several advantages over current electrode-based methods, including enhanced spatial resolution, decreased susceptibility to biological interference, and heightened sensitivity to faint signals. Furthermore, the optical aspect of the optrode provides operational flexibility in terms of wavelength, allowing for versatility in experimental setups. Moreover, its label-free nature and compact size enable seamless integration into multi-channel sensing configurations, enhancing its applicability in multiplexed sensing applications. By leveraging the EO properties of LiNbO₃, the opto-probe can detect changes in the E-field on the order of picometers with a temporal resolution in the nanosecond range. Furthermore, the use of light for measurements eliminates the generation of heat and toxic byproducts, ensuring the safety of the tissue being measured. The analytical and numerical results demonstrate the feasibility and performance of the proposed optrode, with high-quality factor MRRs and high sensitivity to microvolt-level signals. Overall, the findings of this research contribute to the development of a new tool that overcomes the limitations of current electrode-based methods, enabling more accurate and precise measurements of action potentials and providing insights into the intricate dynamics of neuronal networks.

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